Chapter 8

Consensus

8.1 Two Friends

Alice wants to arrange dinner with Bob, and since both of them are very reluctant to use the “call” functionality of their phones, she sends a text message suggesting to meet for dinner at 6pm. However, texting is unreliable, and Alice cannot be sure that the message arrives at Bob’s phone, hence she will only go to the meeting point if she receives a confirmation message from Bob. But Bob cannot be sure that his confirmation message is received; if the confirmation is lost, Alice cannot determine if Bob did not even receive her suggestion, or if Bob’s confirmation was lost. Therefore, Bob demands a confirmation message from Alice, to be sure that she will be there. But as this message can also be lost...

You can see that such a message exchange continues forever, if both Alice and Bob want to be sure that the other person will come to the meeting point!

Remarks:

• Such a protocol cannot terminate: Assume that there are protocols which lead to agreement, and \( P \) is one of the protocols which require the least number of messages. As the last confirmation might be lost, Alice cannot determine if Bob did not even receive her suggestion, or if Bob’s confirmation was lost. Therefore, Bob demands a confirmation message from Alice, to be sure that she will be there. But as this message can also be lost...

• Can Alice and Bob use Paxos?

8.2 Consensus

In Chapter 7 we studied a problem that we vaguely called agreement. We will now introduce a formally specified variant of this problem, called consensus.

Definition 8.1 (consensus). There are \( n \) nodes, of which at most \( f \) might crash, i.e., at least \( n - f \) nodes are correct. Node \( i \) starts with an input value \( v_i \). The nodes must decide for one of those values, satisfying the following properties:

• Agreement All correct nodes decide for the same value.
• Termination All correct nodes terminate in finite time.
• Validity The decision value must be the input value of a node.

Remarks:

• We assume that every node can send messages to every other node, and that we have reliable links, i.e., a message that is sent will be received.
• There is no broadcast medium. If a node wants to send a message to multiple nodes, it needs to send multiple individual messages.
• Does Paxos satisfy all three criteria? If you study Paxos carefully, you will notice that Paxos does not guarantee termination. For example, the system can be stuck forever if two clients continuously request tickets, and neither of them ever manages to acquire a majority.

8.3 Impossibility of Consensus

Model 8.2 (asynchronous). In the asynchronous model, algorithms are event based (“upon receiving message ..., do ...”). Nodes do not have access to a synchronized wall-clock. A message sent from one node to another will arrive in a finite but unbounded time.

Remarks:

• The asynchronous time model is a widely used formalization of the variable message delay model (Model 7.6).

Definition 8.3 (asynchronous runtime). For algorithms in the asynchronous model, the runtime is the number of time units from the start of the execution to its completion in the worst case (every legal input, every execution scenario), assuming that each message has a delay of at most one time unit.

Remarks:

• The maximum delay cannot be used in the algorithm design, i.e., the algorithm must work independent of the actual delay.
• Asynchronous algorithms can be thought of as systems, where local computation is significantly faster than message delays, and thus can be done in no time. Nodes are only active once an event occurs (a message arrives), and then they perform their actions “immediately”.
• We will show now that crash failures in the asynchronous model can be quite harsh. In particular there is no deterministic fault-tolerant consensus algorithm in the asynchronous model, not even for binary input.
Definition 8.4 (configuration). We say that a system is fully defined (at any
point during the execution) by its configuration $C$. The configuration includes
the state of every node, and all messages that are in transit (sent but not yet
received).

Definition 8.5 (univalent). We call a configuration $C$ univalent, if the decision
value is determined independently of what happens afterwards.

Remarks:
- We call a configuration that is univalent for value $v$ $v$-valent.
- Note that a configuration can be univalent, even though no single
  node is aware of this. For example, the configuration in which all
  nodes start with value 0 is 0-valent (due to the validity requirement).
- As we restricted the input values to be binary, the decision value
  of any consensus algorithm will also be binary (due to the validity
  requirement).

Definition 8.6 (bivalent). A configuration $C$ is called bivalent if the nodes
might decide for 0 or 1.

Remarks:
- The decision value depends on the order in which messages are re-
  ceived or on crash events. I.e., the decision is not yet made.
- We call the initial configuration of an algorithm $C_0$. When nodes are
  in $C_0$, all of them executed their initialization code and possibly based
  on their input values, sent some messages. These initial messages are
  also included in $C_0$. In other words, in $C_0$ the nodes are now waiting
  for the first message to arrive.

Lemma 8.7. There is at least one selection of input values $V$ such that the
according initial configuration $C_0$ is bivalent, if $f \geq 1$.

Proof. As explained in the previous remark, $C_0$ only depends on the input values
of the nodes. Let $V = [v_0, v_1, \ldots, v_{n-1}]$ denote the array of input values, where
$v_i$ is the input value of node $i$.

We construct $n+1$ arrays $V_0, V_1, \ldots, V_n$, where the index $i$ in $V_i$ denotes the
position in the array up to which all input values are 1. So, $V_0 = [0, 0, 0, \ldots, 0]$,
$V_1 = [1, 0, 0, \ldots, 0]$, and so on, up to $V_n = [1, 1, 1, \ldots, 1]$.

Note that the configuration corresponding to $V_0$ must be 0-valent so that the
validity requirement is satisfied. Analogously, the configuration corresponding to
$V_n$ must be 1-valent. Assume that all initial configurations with starting values
$V_i$ are univalent. Therefore, there must be at least one index $b$, such
that the configuration corresponding to $V_{b-1}$ is 0-valent, and configuration cor-
responding to $V_b$ is 1-valent. Observe that only the input value of the $b^{th}$ node
differs from $V_{b-1}$ to $V_b$.

Since we assumed that the algorithm can tolerate at least one failure, i.e.,
$f \geq 1$, we look at the following execution: All nodes except $b$ start with their
initial value according to $V_{b-1}$ respectively $V_b$. Node $b$ is “extremely slow”;

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i.e., all messages sent by $b$ are scheduled in such a way, that all other nodes
must assume that $b$ crashed, in order to satisfy the termination requirement.
Since the nodes cannot determine the value of $b$, and we assumed that all initial
configurations are univalent, they will decide for a value $v$ independent of the
initial value of $b$. Since $V_{b-1}$ is 0-valent, $v$ must be 0. However we know that
$V_b$ is 1-valent, thus $v$ must be 1. Since $v$ cannot be both 0 and 1, we have a contradiction.

Definition 8.8 (transition). A transition from configuration $C$ to a following
configuration $C'$ is characterized by an event $\tau = (u, m)$, i.e., node $u$ receiving
message $m$.

Remarks:
- Transitions are the formally defined version of the “events” in the
  asynchronous model we described before.
- A transition $\tau = (u, m)$ is only applicable to $C$, if $m$ was still in transit
  in $C$.
- $C'$ differs from $C$ as follows: $m$ is no longer in transit, $u$ has possibly
  a different state (as $u$ can update its state based on $m$), and there are
  (potentially) new messages in transit, sent by $u$.

Definition 8.9 (configuration tree). The configuration tree is a directed tree
of configurations. Its root is the configuration $C_0$, which is fully characterized
by the input values $V$. The edges of the tree are the transitions; every configuration
has all applicable transitions as outgoing edges.

Remarks:
- For any algorithm, there is exactly one configuration tree for every
  selection of input values.
- Leaves are configurations where the execution of the algorithm termi-
  nated. Note that we use termination in the sense that the system as
  a whole terminated, i.e., there will not be any transition anymore.
- Every path from the root to a leaf is one possible asynchronous exe-
  cution of the algorithm.
- Leaves must be univalent, or the algorithm terminates without agree-
  ment.
- If a node $u$ crashes when the system is in $C$, all transitions $(u, *)$ are
  removed from $C$ in the configuration tree.

Lemma 8.10. Assume two transitions $\tau_1 = (u_1, m_1)$ and $\tau_2 = (u_2, m_2)$ for
$u_1 \neq u_2$ are both applicable to $C$. Let $C_{\tau_1}$ be the configuration that follows $C$
by first applying transition $\tau_1$ and then $\tau_2$, and let $C_{\tau_2\tau_1}$ be defined analogously.
It holds that $C_{\tau_2\tau_1} = C_{\tau_1\tau_2}$.
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Proof. Observe that \( \tau_2 \) is applicable to \( C_{\tau_1} \), since \( m_2 \) is still in transit and \( \tau_1 \) cannot change the state of \( u_0 \). With the same argument \( \tau_1 \) is applicable to \( C_{\tau_2} \), and therefore both \( C_{\tau_1} \) and \( C_{\tau_2} \) are well-defined. Since the two transitions are completely independent of each other, meaning that they consume the same messages, lead to the same state transitions and to the same messages being sent, it follows that \( C_{\tau_1} = C_{\tau_2} \).

Definition 8.11 (critical configuration). We say that a configuration \( C \) is critical, if \( C \) is bivalent, but all configurations that are direct children of \( C \) in the configuration tree are univalent.

Remarks:
- Informally, \( C \) is critical, if it is the last moment in the execution where the decision is not yet clear. As soon as the next message is processed by any node, the decision will be determined.

Lemma 8.12. If a system is in a bivalent configuration, it must reach a critical configuration within finite time, or it does not always solve consensus.

Proof. Recall that there is at least one bivalent initial configuration (Lemma 8.7). Assuming that this configuration is not critical, there must be at least one bivalent following configuration; hence, the system may enter this configuration. But if this configuration is not critical as well, the system may afterwards progress into another bivalent configuration. As long as there is no critical configuration, an unfortunate scheduling (selection of transitions) can always lead the system into another bivalent configuration. The only way how an algorithm can enforce to arrive in a univalent configuration is by reaching a critical configuration.

Therefore we can conclude that a system which does not reach a critical configuration has at least one possible execution where it will terminate in a univalent configuration (hence it terminates without agreement), or it will not terminate at all.

Lemma 8.13. If a configuration tree contains a critical configuration, crashing a single node can create a bivalent leaf; i.e., a crash prevents the algorithm from reaching agreement.

Proof. Let \( C \) denote critical configuration in a configuration tree, and let \( T \) be the set of transitions applicable to \( C \). Let \( \tau_0 = (u_0, m_0) \in T \) and \( \tau_1 = (u_1, m_1) \in T \) be two transitions, and let \( C_{\tau_0} \) be 0-valent and \( C_{\tau_1} \) be 1-valent. Note that \( T \) must contain these transitions, as \( C \) is a critical configuration.

Assume that \( u_0 \neq u_1 \). Using Lemma 8.10 we know that \( C \) has a following configuration \( C_{\tau_0} = C_{\tau_1} \). Since this configuration follows \( C_{\tau_0} \) it must be 0-valent. However, this configuration also follows \( C_{\tau_1} \) and must hence be 1-valent. This is a contradiction and therefore \( u_0 = u_1 \) must hold.

Therefore we can pick one particular node \( u \) for which there is a transition \( \tau = (u, m) \in T \) which leads to a 0-valent configuration. As shown before, all transitions in \( T \) which lead to a 0-valent configuration must also take place on \( u \). Since \( C \) is critical, there must be at least one such transition. Applying the same argument again, it follows that all transitions in \( T \) that lead to a 0-valent configuration must take place on \( u \) as well, and since \( C \) is critical, there is no transition in \( T \) that leads to a bivalent configuration. Therefore all transitions applicable to \( C \) take place on the same node \( u \).

If this node \( u \) crashes while the system is in \( C \), all transitions are removed, and therefore the system is stuck in \( C \), i.e., it terminates in \( C \). But as \( C \) is critical, and therefore bivalent, the algorithm fails to reach an agreement.

Theorem 8.14. There is no deterministic algorithm which always achieves consensus in the asynchronous model, with \( f > 0 \).

Proof. We assume that the input values are binary, as this is the easiest non-trivial possibility. From Lemma 8.7 we know that there must be at least one bivalent initial configuration \( C \). Using Lemma 8.12 we know that if an algorithm solves consensus, all executions starting from the bivalent configuration \( C \) must reach a critical configuration. But if the algorithm reaches a critical configuration, a single crash can prevent agreement (Lemma 8.13).

Remarks:
- If \( f = 0 \), then each node can simply send its value to all others, wait for all values, and choose the minimum.
- But if a single node may crash, there is no deterministic solution to consensus in the asynchronous model.
- How can the situation be improved? For example by giving each node access to randomness, i.e., we allow each node to toss a coin.
8.4 Randomized Consensus

**Algorithm 8.15 Randomized Consensus (Ben-Or)**

1. \( v_i \in \{0, 1\} \) \( \bowtie \) input bit
2. \( \text{round} = 1 \)
3. \( \text{decided} = \text{false} \)
4. Broadcast \( \text{myValue}(v_i, \text{round}) \)
5. while true do
   
   **Propose**
   
   6. Wait until a majority of \( \text{myValue} \) messages of current round arrived
   7. if all messages contain the same value \( v \) then
      
      8. Broadcast \( \text{propose}(v, \text{round}) \)
   9. else
      
      10. Broadcast \( \text{propose}(\neg v, \text{round}) \)
   11. end if
   
   12. if \( \text{decided} \) then
      
      13. Broadcast \( \text{myValue}(v_i, \text{round} + 1) \)
   14. Decide for \( v_i \) and terminate
   15. end if

   **Adapt**
   
   16. Wait until a majority of \( \text{propose} \) messages of current round arrived
   17. if all messages propose the same value \( v \) then
      
      18. \( v_i = v \)
   19. \( \text{decided} = \text{true} \)
   20. else if there is at least one proposal for \( v \) then
      
      21. \( v_i = v \)
   22. else
      
      23. Choose \( v_i \) randomly, with \( Pr[v_i = 0] = Pr[v_i = 1] = 1/2 \)
   24. end if
   25. \( \text{round} = \text{round} + 1 \)
   26. Broadcast \( \text{myValue}(v_i, \text{round}) \)
   27. end while

Remarks:

- The idea of Algorithm 8.15 is very simple: Either all nodes start with the same input bit, which makes consensus easy. Otherwise, nodes toss a coin until a large number of nodes get — by chance — the same outcome.

**Lemma 8.16.** As long as no node sets \( \text{decided} \) to true, Algorithm 8.15 does not get stuck, independent of which nodes crash.

**Proof.** The only two steps in the algorithm when a node waits are in Lines 6 and 16. Since a node only waits for a majority of the nodes to send a message, and since \( f < n/2 \), the node will always receive enough messages to continue, as long as no correct node sets its value decided to true and terminates.

**Lemma 8.17.** Algorithm 8.15 satisfies the validity requirement.

**Proof.** Observe that the validity requirement of consensus, when restricted to binary input values, corresponds to: If all nodes start with \( v \), then \( v \) must be chosen; otherwise, either 0 or 1 is acceptable, and the validity requirement is automatically satisfied.

Assume that all nodes start with 1. In this case, all nodes pose 1 in the first round. As all nodes only hear proposals for 1, all nodes decide for 1 (Line 17) and exit the loop in the following round.

**Lemma 8.18.** Algorithm 8.15 satisfies the agreement requirement.

**Proof.** Observe that proposals for both 0 and 1 cannot occur in the same round, as nodes only send a proposal for \( v \), if they hear a majority for \( v \) in Line 8.

Let \( u \) be the first node that decides for a value \( v \) in round \( r \). Hence, it received a majority of proposals for \( v \) in \( r \) (Line 17). Note that once a node receives a majority of proposals for a value, it will adapt this value and terminate in the next round. Since there cannot be a proposal for any other value in \( r \), it follows that no node decides for a different value in \( r \).

In Lemma 8.16 we only showed that nodes do not get stuck as long as no node decides, thus we need to be careful that no node gets stuck if \( u \) terminates.

Any node \( v' \neq u \) can experience one of two scenarios. Either it also receives a majority for \( v \) in round \( r \) and decides, or it does not receive a majority. In the first case, the agreement requirement is directly satisfied, and also the node cannot get stuck. Let us study the latter case. Since \( u \) heard a majority of proposals for \( v \), it follows that every node hears at least one proposal for \( v \). Hence, all nodes set their value \( v_i \) to \( v \) in round \( r \). Therefore, all nodes will broadcast \( v \) at the end of round \( r \), and thus all nodes will propose \( v \) in round \( r + 1 \). The nodes that already decided in round \( r \) will terminate in \( r + 1 \) and send one additional \( \text{myValue} \) message (Line 13). All other nodes will receive a majority of proposals for \( v \) in \( r + 1 \), and will set decided to true in round \( r + 1 \), and also send a \( \text{myValue} \) message in round \( r + 1 \). Thus, in round \( r + 2 \) some nodes have already terminated, and others hear enough \( \text{myValue} \) messages to continue in Line 8. They send another \( \text{propose} \) and a \( \text{myValue} \) message and terminate in \( r + 2 \), deciding for the same value \( v \).

**Lemma 8.19.** Algorithm 8.15 satisfies the termination requirement, i.e., all nodes terminate in expected time \( O(2^n) \).

**Proof.** We know from the proof of Lemma 8.18 that once a node hears a majority of proposals for a value, all nodes will terminate at most two rounds later. Hence, we only need to show that a node receives a majority of proposals for the same value within expected time \( O(2^n) \).

Assume that no node receives a majority of proposals for the same value. In such a round, some nodes may update their value to \( v \) based on a proposal (Line 20). As shown before, all nodes that update the value based on a proposal, adapt the same value \( v \). The rest of the nodes choose 0 or 1 randomly. The probability that all nodes choose the same value \( v \) in one round is hence at least \( 1/2^n \). Therefore, the expected number of rounds is bounded by \( O(2^n) \). As every round consists of two message exchanges, the asymptotic runtime of the algorithm is equal to the number of rounds.
Theorem 8.20. Algorithm 8.15 achieves binary consensus with expected run-
time $O(2^n)$ if up to $f < n/2$ nodes crash.

Remarks:
- How good is a fault tolerance of $f < n/2$?

Theorem 8.21. There is no consensus algorithm for the asynchronous model
that tolerates $f \geq n/2$ many failures.

Proof. Assume that there is an algorithm that can handle $f = n/2$ many fail-
ures. We partition the set of all nodes into two sets $N, N'$ both containing $n/2$
many nodes. Let us look at three different selection of input values: In $V_0$ all
nodes start with 0. In $V_1$ all nodes start with 1. In $V_{fail}$ all nodes in $N$ start
with 0, and all nodes in $N'$ start with 1.

Assume that nodes start with $V_{fail}$. Since the algorithm must solve consensus
independent of the scheduling of the messages, we study the scenario where
all messages sent from nodes in $N$ to nodes in $N'$ (or vice versa) are heavily
delayed. Note that the nodes in $N$ cannot determine if they started with $V_0$ or
$V_{fail}$. Analogously, the nodes in $N'$ cannot determine if they started in $V_1$ or
$V_{fail}$. Hence, if the algorithm terminates before any message from the other
set is received, $N$ must decide for 0 and $N'$ must decide for 1 (to satisfy the validity
requirement, as they could have started with $V_0$ respectively $V_1$). Therefore,
the algorithm would fail to reach agreement.

The only possibility to overcome this problem is to wait for at least one
message sent from a node of the other set. However, as $f = n/2$ many nodes
can crash, the entire other set could have crashed before they sent any message.
In that case, the algorithm would wait forever and therefore not satisfy the
termination requirement.

Remarks:
- Algorithm 8.15 solves consensus with optimal fault-tolerance – but it
  is awfully slow. The problem is rooted in the individual coin tossing.
  If all nodes toss the same coin, they could terminate in a constant
  number of rounds.
- Can this problem be fixed by simply always choosing 1 at Line 22?!!
- This cannot work: Such a change makes the algorithm deterministic,
  and therefore it cannot achieve consensus (Theorem 8.14). Simulating
  what happens by always choosing 1, one can see that it might happen
  that there is a majority for 0, but a minority with value 1 prevents
  the nodes from reaching agreement.
- Nevertheless, the algorithm can be improved by tossing a so-called
  shared coin. A shared coin is a random variable that is 0 for all nodes
  with constant probability, and 1 with constant probability. Of course,
  such a coin is not a magic device, but it is simply an algorithm. To
  improve the expected runtime of Algorithm 8.15, we replace Line 22
  with a function call to the shared coin algorithm.

8.5 Shared Coin

Algorithm 8.22 Shared Coin (code for node $u$)
1: Choose local coin $c_u = 0$ with probability $1/n$, else $c_u = 1$
2: Broadcast myCoin($c_u$)
3: Wait for $n - f$ coins and store them in the local coin set $C_u$
4: Broadcast mySet($C_u$)
5: Wait for $n - f$ coin sets
6: if at least one coin is 0 among all coins in the coin sets then
7: return 0
8: else
9: return 1
10: end if

Remarks:
- Since at most $f$ nodes crash, all nodes will always receive $n - f$ coins
  respectively coin sets in Lines 3 and 5. Therefore, all nodes make
  progress and termination is guaranteed.
- We show the correctness of the algorithm for $f < n/3$. To simplify
  the proof we assume that $u = 3f + 1, \ i.e., \ we \ assume \ the \ worst \ case.$

Lemma 8.23. Let $u$ be a node, and let $W$ be the set of coins that $u$ received in
at least $f + 1$ different coin sets. It holds that $|W| \geq f + 1$.

Proof. Let $C$ be the multiset of coins received by $u$. Observe that $u$ receives
exactly $|C| = (n - f)^2$ many coins, as $u$ waits for $n - f$ coin sets each containing
$n - f$ coins. Assume that the lemma does not hold. Then, at most $f$ coins are in all $n - f$
coin sets, and all other coins $(n - f)$ are in at most $f$ coin sets. In other words,
the total number of coins that $u$ received is bounded by

$$|C| \leq f \cdot (n - f) + (n - f) \cdot f = 2f(n - f).$$

Our assumption was that $n > 3f$, i.e., $u - f > 2f$. Therefore $|C| \leq 2f(n - f) <
(n - f)^2 = |C|$, which is a contradiction.

Lemma 8.24. All coins in $W$ are seen by all correct nodes.

Proof. Let $w \in W$ be such a coin. By definition of $W$ we know that $w$ is in at
least $f + 1$ sets received by $u$. Since every other node also waits for $n - f$
sets before terminating, each node will receive at least one of these sets, and hence
$w$ must be seen by every node that terminates.

Theorem 8.25. If $f < n/3$ nodes crash, Algorithm 8.22 implements a shared
coin.

Proof. Let us first bound the probability that the algorithm returns 1 for all
nodes. With probability $(1 - 1/n)^n \approx 1/e \approx 0.37$ all nodes chose their local
coin equal to 1 (Line 1), and in that case 1 will be decided. This is only a lower bound on the probability that all nodes return 1, as there are also other scenarios based on message scheduling and crashes which lead to a global decision for 1. But a probability of 0.37 is good enough, so we do not need to consider these scenarios.

With probability $1 - (1 - 1/n)^W$ there is at least one 0 in $W$. Using Lemma 8.23 we know that $|W| \geq f + 1 \approx n/3$, hence the probability is about $1 - (1 - 1/n)^{n/3} \approx 1 - (1/e)^{1/3} \approx 0.28$. We know that this 0 is seen by all nodes (Lemma 8.24), and hence everybody will decide 0. Thus Algorithm 8.22 implements a shared coin.

Remarks:
- We only proved the worst case. By choosing $f$ fairly small, it is clear that $f + 1 \neq n/3$. However, Lemma 8.23 can be proved for $|W| \geq n - 2f$. To prove this claim you need to substitute the expressions in the contradictory statement: At most $n - 2f - 1$ coins can be in all $n - f$ coin sets, and $n - (n - 2f - 1) = 2f + 1$ coins can be in at most $f$ coin sets. The remainder of the proof is analogous, the only difference is that the math is not as neat. Using the modified Lemma we know that $|W| \geq n/3$, and therefore Theorem 8.25 also holds for any $f < n/3$.
- We implicitly assumed that message scheduling was random; if we need a 0 but the nodes that want to propose 0 are “slow”, nobody is going to see these 0’s, and we do not have progress. There exist more complicated protocols that solve this problem.

Theorem 8.26. Plugging Algorithm 8.22 into Algorithm 8.15 we get a randomized consensus algorithm which terminates in a constant expected number of rounds tolerating up to $f < n/3$ crash failures.

Chapter Notes

The problem of two friends arranging a meeting was presented and studied under many different names; nowadays, it is usually referred to as the Two Generals Problem. The impossibility proof was established in 1975 by Akkoyunlu et al. [AEH75].

The proof that there is no deterministic algorithm that always solves consensus is based on the proof of Fischer, Lynch and Paterson [FLP85], known as FLP, which they established in 1985. This result was awarded the 2001 PODC Influential Paper Award (now called Dijkstra Prize). The idea for the randomized consensus algorithm was originally presented by Ben-Or [Ben83]. The concept of a shared coin was introduced by Bracha [Bra87]. A shared coin that can withstand worst-case scheduling has been developed by Alistarh et al. [AAKS14]; this shared coin was inspired by earlier shared coin solutions in the shared memory model [Cha96].

Apart from randomization, there are other techniques to still get consensus. One possibility is to drop asynchrony and rely on time more, e.g. by assuming partial synchrony [DLS88] or timed asynchrony [CF98]. Another possibility is to add failure detectors [CT96].

This chapter was written in collaboration with David Stolz.

Bibliography


